

Appendix C

Answers to Selected Exercises

CHAPTER 2

Section 2-1

- 2-1.** Let a , b denote a part above, below the specification.

$$S = \{aaa, aab, aba, abb, baa, bab, bba, bbb\}$$

- 2-7.** S is the sample space of 100 possible two-digit integers.

- 2-9.** $S = \{0, 1, 2, \dots\}$ in ppb.

- 2-17.** $c = \text{connect}$, $b = \text{busy}$, $S = \{c, bc, bbc, bbhc, bbbhc, \dots\}$

- 2-21.** (a) $S = \{0, 1, 2, 3, \dots\}$
 (b) S (c) $\{12, 13, 14, 15\}$
 (d) $\{0, 1, 2, \dots, 11\}$ (e) S
 (f) $\{0, 1, 2, \dots, 7\}$ (g) \emptyset
 (h) \emptyset (i) $\{8, 9, 10, \dots\}$

- 2-23.** Let d denote a distorted bit and let o denote a bit that is not distorted.

$$(a) S = \left\{ \begin{array}{l} dddd, dodd, oddd, oodd, \\ dddo, dodo, oddo, oodo, \\ ddod, dood, odod, oood, \\ ddoo, dooo, odoo, oooo \end{array} \right\}$$

(b) No

$$(c) \{dddd, dodd, dddo, dodo, ddod, dood, ddoo, dooo\}$$

- (d) $\{oddd, oodd, oddo, oodo, odod, oood, odoo, oooo\}$
 (e) $\{dddd\}$
 (f) $\{dddd, dodd, dddo, oddd, ddod, oodd, ddoo\}$

$$2-25. 2^{12} = 4096$$

- 2-27.** (a) $A' \cap B = 10$, $B' = 10$, $A \cup B = 92$

- 2-29.** (a) $A' = \{x \mid x \geq 72.5\}$
 (b) $B' = \{x \mid x \leq 52.5\}$
 (c) $A \cap B = \{x \mid 52.5 < x < 72.5\}$
 (d) $A \cup B = \{x \mid x > 0\}$

- 2-31.** Let g denote a good board, m a board with minor defects, and j a board with major defects.

$$(a) S = \{gg, gm, gj, mg, mm, mj, jg, jm, jj\}$$

$$(b) S = \{gg, gm, gj, mg, mm, mj, jg, jm\}$$

Section 2-2

- 2-35.** (a) 0.4 (b) 0.8 (c) 0.6
 (d) 1 (e) 0.2

- 2-37.** (a) $S = \{1, 2, 3, 4, 5, 6, 7, 8\}$
 (b) $2/8$ (c) $6/8$

- 2-39.** (a) 0.7 (b) 0.8

- 2-41.** (a) 0.25 (b) 0.75

$$2-43. 5.7 \times 10^{-8}$$

- 2-45.** (a) 0.86 (b) 0.79 (c) 0.14
 (d) 0.70 (e) 0.95 (f) 0.84

- 2-47.** (a) 0.30 (b) 0.77 (c) 0.70
 (d) 0.22 (e) 0.85 (f) 0.92

Section 2-3

- 2-49.** (a) 0.7 (b) 0.4 (c) 0.1
 (d) 0.2 (e) 0.6 from part (b)
 (f) 0.8

- 2-51.** No

- 2-53.** (a) $350/370$ (b) $362/370$
 (c) $358/370$ (d) $345/370$

- 2-55.** (a) $13/130$ (b) No

Section 2-4

- 2-57.** (a) $86/100$ (b) $P(B) = 79/100$ (c) $70/79$
 (d) $70/86$

- 2-59.** (a) $345/357$ (b) $5/13$

- 2-61.** (a) 0.15 (b) 0.153
 (c) 0.72 (d) 0.733
 (e) 0.11 (f) 0.76

- 2-63.** (a) $15/40$ (b) $14/39$
 (c) 0.135 (d) 0.599

- 2-65.** (a) $4/499 = 0.0080$
 (b) $(5/500)(4/499) = 0.000080$
 (c) $(495/500)(494/499) = 0.98$
- 2-67.** (a) 0.813 (b) 0.632
 (c) 0.764

Section 2-5

- 2-71.** 0.22
- 2-73.** 0.023
- 2-75.** 0.028
- 2-77.** (a) 0.0225 (b) 0.125
- 2-79.** (a) 0.20 (b) 0.20

Section 2-6

- 2-81.** No
- 2-83.** No
- 2-85.** (a) No (b) 0.733
- 2-87.** (a) 0.59 (b) 0.328 (c) 0.41
- 2-89.** (a) 0.00003 (b) 0.00024
 (c) 0.00107
- 2-91.** 0.9702
- 2-93.** (a) No (b) Yes

Section 2-7

- 2-95.** 0.003
- 2-97.** (a) 0.615 (b) 0.618
 (c) 0.052
- 2-99.** (a) 0.9847 (b) 0.1184

Supplemental

- 2-101.** The sample space $S = \{A, A'D_1, A'D_2, A'D_3, A'D_4, A'D_5\}$
- 2-103.** (a) 0.19 (b) 0.15 (c) 0.99
 (d) 0.80 (e) 0.158
- 2-105.** (a) No (b) No (c) 40/240
 (d) 200/240 (e) 234/400
 (f) 1
- 2-107.** (a) 0.282 (b) 0.718
- 2-109.** 0.996
- 2-111.** (a) 0.0037 (b) 0.811
- 2-113.** (a) 0.0778 (b) 0.00108
 (c) 0.947
- 2-115.** (a) 0.9764 (b) 0.680
- 2-117.** (a) 0.207 (b) 0.625 (c) 0.6
- 2-119.** (a) 0.453 (b) 0.261
 (c) 0.881 (d) 0.547
 (e) 0.783 (f) 0.687
- 2-121.** 1.58×10^{-7}

CHAPTER 3**Section 3-1**

- 3-1.** $\{0, 1, 2, \dots, 1000\}$
- 3-3.** $\{0, 1, 2, \dots, 99999\}$

Section 3-2

- 3-13.** $f_X(0) = 1/3, f_X(1.5) = 1/3,$
 $f_X(2) = 1/6, f_X(3) = 1/6$
- 3-15.** (a) 1 (b) $7/8$ (c) $3/4$
 (d) $1/2$
- 3-17.** (a) $9/25$ (b) $4/25$
 (c) $12/25$ (d) 1
- 3-19.** $P(X = 10 \text{ million}) = 0.3,$
 $P(X = 5 \text{ million}) = 0.6,$
 $P(X = 1 \text{ million}) = 0.1$
- 3-21.** $P(X = 0) = 8 \times 10^{-6},$
 $P(X = 1) = 0.0012,$
 $P(X = 2) = 0.0576,$
 $P(X = 3) = 0.9412$
- 3-23.** $P(X = 15 \text{ million}) = 0.6,$
 $P(X = 5 \text{ million}) = 0.3,$
 $P(X = -0.5 \text{ million}) = 0.1$
- 3-25.** $P(X = 0) = 0.00001,$
 $P(X = 1) = 0.00167,$
 $P(X = 2) = 0.07663,$
 $P(X = 3) = 0.92169$

Section 3-3

- 3-27.** (a) $7/8$ (b) 1 (c) $3/4$
 (d) $3/8$
- 3-29.** $F(x) = 0 \text{ for } x < 1 \text{ million}; 0.1$
 for $1 \text{ million} \leq x < 5 \text{ million};$
 0.7 for $5 \text{ million} \leq x < 10 \text{ million};$
 1 for $10 \text{ million} \leq x$
- 3-31.** $F(x) = 0 \text{ for } x < 0;$ 0.008 for
 $0 \leq x < 1;$ 0.104 for $1 \leq x < 2;$
 0.488 for $2 \leq x < 3;$ 1 for $3 \leq x$
- 3-33.** (a) 1 (b) 0.5 (c) 0.5
 (d) 0.5
- 3-35.** (a) 1 (b) 0.75 (c) 0.25
 (d) 0.25 (e) 0 (f) 0

Section 3-4

- 3-37.** $E(X) = 2, V(X) = 2$
- 3-39.** $E(X) = 0, V(X) = 1.5$
- 3-41.** $E(X) = 6.1 \text{ million},$
 $V(X) = 7.89 \text{ million}^2$
- 3-43.** $E(X) = 2.4, V(X) = 0.48$
- 3-45.** $x = 24$

Section 3-5

- 3-47.** $E(X) = 2, V(X) = 0.667$
- 3-49.** $E(X) = 0.17, V(X) = 0.0002$
- 3-51.** $E(X) = 590.45, V(X) = 0.0825$

Section 3-6

- 3-57.** (a) 0.2461 (b) 0.0547
 (c) 0.0107 (d) 0.3223

- 3-59.** (a) 2.4×10^{-8} (b) 0.99989
 (c) 9.91×10^{-18}
 (d) 1.138×10^{-4}

- 3-61.** $F(x) = 0 \text{ for } x < 0;$ 0.4219 for
 $0 \leq x < 1;$ 0.8438 for $1 \leq x < 2;$
 0.9844 for $2 \leq x < 3;$ 1 for $3 \leq x$

- 3-63.** (a) 0.3681 (b) 0.6323
 (c) 0.9198 (d) $E(X) = 1,$
 $V(X) = 0.999$

- 3-65.** (a) $n = 50, p = 0.1$
 (b) 0.1117 (c) 4.51×10^{-48}

- 3-67.** (a) 0.9961 (b) 0.9886
3-69. (a) 0 (b) 0.2137

Section 3-7

- 3-71.** (a) 0.5 (b) 0.0625
 (c) 0.0039 (d) 0.75 (e) 0.25
- 3-73.** (a) 0.0064 (b) 0.9984
 (c) 0.008
- 3-75.** (a) 0.0167 (b) 0.9224 (c) 50
- 3-77.** (a) 3.91×10^{-19} (b) 200
 (c) 2.56×10^{18}
- 3-79.** (a) 5 (b) 5
- 3-81.** (a) 20 (b) 0.0436
 (c) 0.0459 (d) 0.0411 (e) 19
- 3-83.** (a) 3000 (b) 1431.18

Section 3-8

- 3-87.** (a) 0.4623 (b) 0.0002
 (c) 0.9866 (d) $E(X) = 0.8,$
 $V(X) = 0.539$
- 3-89.** $F(X) = 0 \text{ for } x < 0;$ 1/6 for $0 \leq x < 1;$ 2/3 for $1 \leq x < 2;$ 29/30 for $2 \leq x < 3;$ 1 for $3 \leq x$
- 3-91.** (a) 0.1201 (b) 0.8523
- 3-93.** (a) 0.7069 (b) 0.0607
 (c) 0.2811

Section 3-9

- 3-97.** (a) 0.0183 (b) 0.2381
 (c) 0.1954 (d) 0.0298
- 3-99.** $E(X) = 2.996, V(X) = 2.996$
- 3-101.** (a) 0.0045 (b) 0.3679
 (c) 0.1353 (d) 0.2642
- 3-103.** (a) 4.54×10^{-5} (b) 0.6321
- 3-105.** (a) 0.6065 (b) 8.9×10^{-5}
 (c) 0.00146

Supplemental

- 3-107.** 0.3714
- 3-109.** (a) 0.0117 (b) 1.3333
- 3-111.** (a) 0.1755 (b) 0.0858
 (c) 0.2873
- 3-113.** 0.9810

3-115.

x	2	3	4	5	6
$f(x)$	0.0025	0.01	0.03	0.065	0.13

x	7	8	9	10
$f(x)$	0.18	0.2225	0.2	0.16

3-117. 299**3-119.** (a) 4.1×10^{-5} (b) 10
(c) 0.9995**3-121.** (a) 0.6 (b) 0.8 (c) 0.7
(d) 3.9 (e) 3.09**3-123.** (a) 0.2408 (b) 0.4913**3-125.** (a) 0.3233 (b) 0.0916**3-127.** 0.0738**3-129.** (a) 0.3679 (b) 50.51
(c) 0.9234

CHAPTER 4

Section 4-2

4-1. (a) 0.3670 (b) 0.2858 (c) 0
(d) 0.9817 (e) 0.0498**4-3.** (a) 0.4375 (b) 0.7969
(c) 0.5625 (d) 0.7031
(e) 0.5**4-5.** (a) 0.5 (b) 0.4375 (c) 0.125
(d) 0 (e) 1 (f) 0.9655**4-7.** (a) 0.5 (b) 49.8**4-9.** (a) 0.10 (b) 2.5

Section 4-3

4-11. (a) 0.56 (b) 0.7 (c) 0 (d) 0**4-13.** $1 - e^{-x}$ for $x > 0$ **4-15.** $1 - e^{-(x-4)}$ for $x > 4$ **4-17.** (a) $1.25x - 93.25$ for
 $74.6 < x < 75.4$ (b) 0.5**4-21.** $F(x) = 0$ for $x < 0$; $0.25x^2$ for
 $0 \leq x < 2$; 1 for $x \leq 2$

Section 4-4

4-23. $E(X) = 2.6667$, $V(X) = 0.8889$ **4-25.** $E(X) = 4.083$, $V(X) = 0.3291$ **4-27.** (a) $E(X) = 109.39 \mu\text{m}$,
 $V(X) = 33.19 \mu\text{m}^2$
(b) \$54.70**4-29.** (a) $E(X) = 5.1 \text{ mm}$, $V(X) = 0.01 \text{ mm}^2$ (b) 0.3679

Section 4-5

4-31. (a) $E(X) = 3.5$, $V(X) = 1.33$,
 $\sigma_X = 1.155$ (b) 0.25**4-33.** (a) $E(X) = 50$, $V(X) = 0.0208$,
 $\sigma_X = 0.144$ (b) $F(x) = 2x$
-99.5 for $49.75 < x < 50.25$
(c) 0.7**4-35.** (a) $E(X) = 1.85 \text{ min}$, $V(X) = 0.0408 \text{ min}^2$ (b) 0.7143
(c) $F(x) = (x - 1.5)/0.7$ for
 $1.5 < x < 2.2$ **4-37.** (b) 0.25 (c) 0.2140
(d) $E(X) = 0.2100 \mu\text{m}$,
 $V(X) = 0.00000833 \mu\text{m}^2$

Section 4-6

4-39. (a) 0.90658 (b) 0.99865
(c) 0.07353 (d) 0.98422
(e) 0.95116**4-41.** (a) 1.28 (b) 0 (c) 1.28
(d) -1.28 (e) 1.33**4-43.** (a) 0.93319 (b) 0.69146
(c) 0.9545 (d) 0.00135
(e) 0.15866**4-45.** (a) 0.93319 (b) 0.89435
(c) 0.38292 (d) 0.80128
(e) 0.54674**4-47.** (a) 0.99379 (b) 0.13591
(c) 5835**4-49.** (a) 0.0082 (b) 0.72109
(c) 0.564**4-51.** (a) 0.00135 (b) 0.15866
(c) 71.6 min**4-53.** (a) 0.02275 (b) 0.47725
(c) 0.336**4-55.** (a) 0.15866 (b) 90.0
(c) 99.73%**4-57.** (a) 0.15245 (b) 125.6**4-59.** (a) 0.06681 (b) 0.86638
(c) 0.000214

Section 4-7

4-61. (a) 0.075 (b) 0.85**4-63.** (a) 0.129 (b) 0.488**4-65.** 0.013**4-67.** 0.966**4-71.** (b) 330 (c) 0.0089

Section 4-9

4-73. (a) 0.3679 (b) 0.1353
(c) 0.0498 (d) 29.96**4-75.** (a) 0.333 min (b) 0.333 min
(c) 0.9986**4-77.** (a) 0.1353 (b) 0.4866
(c) 0.2031 (d) 34.54**4-79.** (a) 0.0498 (b) 0.8775**4-81.** (a) 0.0025 (b) 0.6321**4-83.** (a) 0.1353 (b) 0.2707 (c) 5**4-85.** (a) 0.2212 (b) 0.2865
(c) 0.2212**4-87.** 0.8488**4-93.** (a) 5 (b) 0.1353 (c) No
(d) 11.51

Section 4-10

4-97. (a) 0.1755 (b) 0.2643**4-99.** (a) 50,000 (b) 0.677**4-101.** (a) 500,000 (b) 223607
(c) 0.0803**4-103.** (a) 0.1429 (b) 0.1847**4-105.** (a) 120 (b) 1.32934
(c) 11.6317

Section 4-11

4-109. (a) 12,000 (b) 3.61×10^{10} **4-111.** (a) 0.5273 (b) 8862.3
(c) 0.00166**4-113.** (a) 0.275 (b) 0.685**4-115.** (a) 443.11 (b) 53650.5
(c) 0.2212

Section 4-12

4-117. (a) 0.9332 (b) 20952.2
(c) $E(X) = 13359.7$, $V(X) = 1.45 \times 10^{12}$ **4-119.** (a) 0.983 (b) 0.45**4-121.** $\theta = 3.45$, $\omega^2 = 2.25$

Supplemental

4-125. $0.25x^2 - x + 1$ for $2 < x < 4$ **4-127.** (a) 0.3935 (b) 0.3834
(c) 23.03**4-129.** (a) 0.423 (b) 50**4-133.** (a) $\theta = 3.43$, $\omega^2 = 0.96$
(b) 0.946**4-135.** (a) 0.6915 (b) 0.683
(c) 1.86**4-137.** (a) 0.0062 (b) 0.0124
(c) 5.33**4-139.** 0.0008 to 0.0032**4-141.** $\mu = 11,398$ **4-143.** (a) 0.5633 (b) 737.5**4-145.** (a) 0.984 (b) 0.834

CHAPTER 5

Section 5-1

5-1. $f(x, y) \geq 0$, $\sum f(x, y) = 1$ **5-3.** $E(X) = 1.8125$, $E(Y) = 2.875$ **5-5.** $c = 1/36$ **5-7.** $E(X) = 2.167$, $V(X) = 0.639$,
 $E(Y) = 2.167$, $V(Y) = 0.639$

5-9. $f(x, y) \geq 0, \sum f(x, y) = 1$ **5-11.** $E(X) = 1/8, E(Y) = 1/4$ **5-13.** $X \geq 0, Y \geq 0$ and $X + Y \leq 4$ **5-15.** (b) $f_X(0) = 0.2338, f_X(1) = 0.4188, f_X(2) = 0.2679, f_X(3) = 0.0725, f_X(4) = 0.0070$ (c) $E(X) = 1.2$ (d) $f_{Y|3}(0) = 0.857, f_{Y|3}(1) = 0.143,$ (e) $E(Y|X = 3) = 0.143$ **Section 5-2****5-17.** (a) 0.5 (b) 0.35 (c) 0.5
(d) 0.8 (e) 1.5**5-19.** $P(X = 1 | Y = 1, Z = 2) = 0.4, P(X = 2 | Y = 1, Z = 2) = 0.6$ **5-21.** (a) 0 (b) 0.072 (c) 0.736
(d) 1**5-23.** (a) $x \geq 0, y \geq 0, z \geq 0, x + y + z = 4$
(b) No**5-25.** (a) 0.1758 (b) 0.2198
(c) $E(X) = 1.067, V(X) = 0.6146$ **5-27.** (a) Yes (b) 0.1944
(c) 0.0001**5-29.** (a) 0.7347 (b) 0(c) $P(X = 0 | Y = 2) = 0.0204, P(X = 1 | Y = 2) = 0.2449, P(X = 2 | Y = 2) = 0.7347$ (c) $E(X | Y = 2) = 1.7142$ **5-31.** (a) binomial $p = 0.03, n = 3$
 $E(X) = 0.03, V(X) = 0.0297$
(b) $P(X = 0 | Y = 2) = 0.98958, P(X = 1 | Y = 2) = 0.01042$
(c) $E(X | Y = 2) = 0.01042, V(X | Y = 2) = 0.01031$ **Section 5-3****5-35.** (a) 0.4444 (b) 0.6944
(c) 0.5833 (d) 0.3733 (e) 2
(f) 0**5-37.** 1/24**5-39.** (a) $(2x + 1)/12$ for $0 < x < 3$
(b) $(y + 1)/6$ for $1 < y < 3$
(c) 2.111

(d) 0.4167

(e) $(2 + x)/6$ for $0 < x < 2$ **5-43.** 10**5-45.** (a) $10(e^{-2x} - e^{-5x})/3$ for $0 < x$
(b) $3.157e^{-3y}$ for $0 < y < 1$
(c) 0.089 (d) $2e^{-2x+4}$ for $2 < x$ **5-49.** 2/15**5-51.** (a) $(x + 1)/7.5$ for $0 < x < 1, 2/7.5$ for $1 < x < 4$ (b) 0.5 for $0 < y < 2$

(c) 1 (d) 0.25

5-53. (a) 0.0439, 0.0019

(b) 0.065

Section 5-4**5-55.** (a) 0.25 (b) 0.0625 (c) 1
(d) 1 (e) 2/3**5-57.** (a) $2x$ for $0 < x < 1$

(b) 0.25

5-61. 6**5-63.** (a) $3(x - 1)^2$ for $0 < x < 1$ (b) $6(1 - x - y)$ for $0 < x, 0 < y$ and $x + y < 1$ (c) 1 for $x = 0$ (d) $4(1 - 2x)$ for $x < 0.5$ **5-65.** (a) 0.032 (b) 0.0267**Section 5-5****5-67.** $\sigma_{XY} = 0.703, \rho_{XY} = 0.885$ **5-69.** $c = 1/36, \sigma_{XY} = -1/36, \rho_{XY} = -0.0435$ **5-71.** $\sigma_{XY} = -1/3, \rho_{XY} = -1/2$ **5-73.** $c = 9.5, \sigma_{XY} = 1.852, \rho_{XY} = 0.928$ **5-75.** X and Y are independent and $\sigma_{XY} = \rho_{XY} = 0$ **Section 5-6****5-81.** 0.827**Section 5-7****5-87.** (a) 30 (b) 97 (c) 0.5
(d) 0.846**5-89.** (a) $E(T) = 4, \sigma_T = 0.1414$

(b) 0.017

5-91. (a) $E(D) = 1/8, \sigma_D = 0.140$
(b) 0.187 (c) 0.187**5-93.** (a) 0.05 (b) 0.023

(c) 12.129

(d) 0.388 (e) 136

5-95. (a) 0.023 (b) 4558**Supplemental****5-97.** (a) 3/8 (b) 3/4 (c) 3/4

(d) 3/8

(e) $E(X) = 7/8, V(X) =$ 39/64, $E(Y) = 7/8, V(Y) = 39/64$ **5-99.** (a) 0.0631 (b) 0.122(c) $E(X) = 2, V(X) = 1.8$
(d) $f_{X|19}(0) = 0.667, f_{X|19}(1) = 0.333$

(e) 1/3

5-103. (b) 1/3 (c) No**5-105.** (a) 0.0093 (b) 0.5787

(c) 0.75 (d) 0.2199

(e) 2.25 (f) 1.3333

5-107. (a) $1/2$ (b) $1/4$ (c) $1/\pi$ for $x^2 + y^2 \leq 1$
(d) $2\sqrt{1 - x^2}/\pi$ for $-1 < x < 1$ **5-109.** 3/4**5-111.** (a) 0.085 (b) $\text{Bin}(10, 0.3)$
(c) 3**5-113.** (a) 0.499 (b) 0.5**5-115.** (a) 0.057 (b) 0.057**5-119.** (a) $E(T) = 1.5, V(T) = 0.078$
(b) ≈ 0 (c) $E(P) = 4, V(P) = 0.568$ **5-121.** $\mu = 5, \sigma = \sqrt{3}$ **CHAPTER 6****Section 6-1****6-1.** $\bar{x} = 74.0044, s = 0.00473$ **6-3.** $\bar{x} = 7068.1, s = 226.5$ **6-5.** $\bar{x} = 43.975, s = 12.294$ **6-7.** $\mu = 5.44$ **6-11.** (a) $\bar{x} = 7.184$ (b) $s = 0.02066$ **6-13.** (a) $\bar{x} = 65.85, s = 12.16$ (c) $\bar{x} = 66.86, s = 10.74$ **Section 6-3****6-19.**Variable N Median Q1 Q3
cycles 70 1436.5 1097.8 1735.0**6-21.**Variable N Median Q1 Q3
yield 90 89.250 86.100 93.125**6-25.** $\bar{x} = 260.7, s = 13.03$, and $\tilde{x} = 261.15$ **6-27.** (b) $\bar{x} = 89, s = 2.8$, and $\tilde{x} = 90$ (c) 22/40**Section 6-5****6-43.** (a) $\bar{x} = 4.0$ (b) $s^2 = 0.867, s = 0.931$ **6-45.** (a) $\bar{x} = 952.44, s^2 = 9.55, s = 3.09$ (b) $\tilde{x} = 953$, largest value can increase by any amount

- 6-47.** (a) $\bar{x} = 48.125$, $\tilde{x} = 49$
 (b) $s^2 = 7.246$, $s = 2.692$

Supplemental

- 6-73.** (a) $\bar{x} = 65.083$
 (b) $s^2 = 1.86869$, $s = 1.367$
- 6-75.** (a) Sample 1: range = 4;
 Sample 2: range = 4
 (b) Sample 1: $s = 1.604$;
 Sample 2: $s = 1.852$
- 6-79.** (b) $\bar{x} = 9.325$, $s = 4.48586$

CHAPTER 7**Section 7-2**

- 7-1.** Estimator 1
- 7-3.** Estimator 2
- 7-5.** 2.5
- 7-7.** Estimator 3 is most efficient;
 estimator 2 is the best “unbiased”
 estimator.
- 7-11.** (a) 75.427 (b) 75.1
 (c) $\sigma^2 = 2.214$, $\sigma = 1.488$
 (d) 0.292 (e) 0.0385
- 7-13.** (a) Yes (b) $\frac{1}{\sqrt{2}} \sigma$

7-15. (b) $se = \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$

7-17. (b)
 $se(\hat{\mu}) = \sigma_1 \sqrt{\frac{\alpha^2 n_2 + (1 - \alpha)^2 a n_1}{n_1 n_2}}$

(c) $\alpha = \frac{a n_1}{n_2 + a n_1}$ (d) 0.10

Section 7-3

- 7-31.** (a) 423.33, 82.4464

Section 7-5

- 7-33.** 0.8385
- 7-35.** 0.43055
- 7-37.** 0.3472
- 7-39.** 12
- 7-41.** 0.2313
- 7-43.** (a) 0.5885
 (b) 0.1759
- 7-45.** 0.983

Supplemental

- 7-49.** $\bar{X}_1 - \bar{X}_2 \sim N(-5, 0.2233)$
- 7-51.** 0.8664
- 7-53.** 1 (approximately)
- 7-55.** 0 (approximately)

CHAPTER 8**Section 8-2**

- 8-1.** 97.93%, 99.36%, and 96.78%
- 8-3.** (a) 1.29 (b) 1.65 (c) 2.33
- 8-5.** 3
- 8-7.** (a) Longer (b) No
 (c) Yes
- 8-9.** (89.471, 91.489)
- 8-11.** (a) (74.0353, 74.0367)
 (b) (74.0355, ∞)
- 8-13.** (a) (3232.11, 3267.89)
 (b) (3226.5, 3273.5)
- 8-15.** 267
- 8-17.** 4

Section 8-3

- 8-19.** $t_{0.025,15} = 2.131$, $t_{0.05,10} = 1.812$,
 $t_{0.10,20} = 1.325$, $t_{0.005,25} = 2.787$,
 $t_{0.001,30} = 3.385$
- 8-21.** (a) $t_{0.05,14} = 1.761$
 (b) $t_{0.01,19} = 2.359$
 (c) $t_{0.001,24} = 3.467$
- 8-23.** (1.108, ∞)
- 8-25.** (a) Yes (b) (16.455, 17.505)
- 8-27.** (a) Yes (b) (8.216, 8.244)
- 8-29.** (4.023, ∞)
- 8-31.** (1.093, 1.106)

Section 8-4

- 8-33.** $\chi^2_{0.05,10} = 18.31$,
 $\chi^2_{0.025,15} = 27.49$,
 $\chi^2_{0.01,12} = 26.22$,
 $\chi^2_{0.005,25} = 46.93$,
 $\chi^2_{0.95,20} = 10.85$,
 $\chi^2_{0.99,18} = 7.01$,
 $\chi^2_{0.995,16} = 5.14$
- 8-35.** $0.00003075 < \sigma^2$
- 8-37.** $7.975, 727.09 < \sigma^2$
- 8-39.** $0.31 < \sigma < 0.46$
- 8-41.** $3.8 \leq \sigma$

Section 8-5

- 8-43.** 622
- 8-45.** 666
- 8-47.** 5759

Section 8-6

- 8-49.** $52131.1 \leq X_{n+1} \leq 68148.3$
- 8-51.** $263.5 \leq X_{n+1} \leq 370.9$
- 8-53.** $2193.5 \leq X_{n+1} \leq 2326.5$
- 8-55.** $3.19 \leq X_{n+1} \leq 4.19$
- 8-57.** $2.56 \leq X_{n+1} \leq 3.22$
- 8-59.** $228.1 \leq X_{n+1} \leq 235.2$

Section 8-7

- 8-61.** (0.408, 2.092)
- 8-63.** (15.14, 18.82)
- 8-65.** (8.16, 8.30)
- 8-67.** (3.91, ∞)
- 8-69.** (1.06, 1.14)

Supplemental

- 8-71.** (a) $0.1 \leq P\text{-value} \leq 0.25$
 (b) $0.05 \leq P\text{-value} \leq 0.1$
 (c) $P\text{-value} = 0.00539$
- 8-75.** (a) 40 (b) 23
- 8-77.** $2178.51 \leq X_{n+1} \leq 2341.49$
- 8-79.** (a) Yes
 (b) $0.618 \leq \mu \leq 0.630$
 (c) $0.588 \leq X_{n+1} \leq 0.660$
 (d) (0.583, 0.665)
- 8-81.** (a) Yes
 (b) $2.270 \leq \mu \leq 4.260$
 (c) $-1.297 \leq X_{n+1} \leq 7.827$
 (d) (-3.113, 10.363)
- 8-83.** (a) $0.0021 \leq p \leq 0.0088$
 (b) Yes
- 8-85.** (a) $0.210 \leq p \leq 0.274$
 (b) $0.204 \leq p \leq 0.280$

CHAPTER 9**Section 9-1**

- 9-1.** (a) Yes (b) No (c) No
 (d) No (e) No
- 9-3.** (a) 0 (b) 0.02275
- 9-5.** 11.5875
- 9-7.** (a) 0.09296 (b) 0.04648
 (c) 0.00005
- 9-9.** (a) Reject H_0 (b) 0.00889
- 9-11.** (a) 182.9 (b) 0.00776
- 9-13.** (a) 0.0164 (b) 0.21186
- 9-17.** (a) 0.08535 (b) 0
- 9-19.** (a) 0.29372 (b) 0.25721

Section 9-2

- 9-21.** (a) $z_0 = 0.36$, do not reject H_0
 (b) $P\text{-value} = 0.71884$ (c) 5
 (d) 0.68054 (e) (87.85, 93.11)
- 9-23.** (a) $z_0 = -1.69$, do not reject H_0
 (b) 0.091028 (c) 0 (d) 1
- 9-25.** (a) $z_0 = -14.43$, reject H_0
 (b) 0 (c) (3232.11, 3267.89)
- 9-27.** (a) $z_0 = 1.55$, do not reject H_0
 (b) 0.02938 (c) 1
 (d) (99.888, ∞)
- 9-29.** (a) $z_0 = 1.77$, reject H_0 (b) 1
 (c) 35 (d) (4.003, ∞)

Section 9-3

- 9-31.** (a) $t_0 = -3.48$, reject H_0 ,
 P -value = 0.002
(b) 1 (c) 35
(d) (98.065, 98.463)
(e) Yes
- 9-33.** (a) $t_0 = -1.46$, do not reject H_0 , P -value = 0.156
(b) Yes (c) 0.85 (d) 51
(e) (129.406, 130.100)
- 9-35.** $t_0 = 4.47$, reject H_0 ,
 P -value < 0.0005
- 9-37.** (a) $t_0 = -5.35$, do not reject H_0
(b) P -value > 0.4
(c) 0.75 (d) 38
- 9-39.** (a) $t_0 = 2.806$, reject H_0
(b) P -value = 0.004 (c) 1
(d) 3
- 9-41.** (a) $t_0 = 3.018$, reject H_0
(b) P -value = 0.0038 (c) 0.8
(d) 38

Section 9-4

- 9-43.** (a) $\chi^2_0 = 8.96$, do not reject H_0
(b) $0.5 < P$ -value < 0.9
(c) 50
- 9-45.** (a) $\chi^2_0 = 4984.83$, reject H_0
(b) P -value < 0.005
- 9-47.** (a) $\chi^2_0 = 109.52$, reject H_0
(b) $0.31 < \sigma < 0.46$
- 9-49.** 30

Section 9-5

- 9-51.** 0.639, 118
- 9-53.** (a) $z_0 = -0.53$, do not reject H_0
(b) P -value = 0.29806
- 9-55.** (a) $z_0 = 0.452$, do not reject H_0
(b) P -value = 0.67364
- 9-57.** (a) $\alpha = 0.0853$ (b) $\beta \cong 0$

Section 9-7

- 9-59.** (a) $\chi^2_0 = 7.2$, do not reject H_0
(b) $0.05 < P$ -value < 0.10
- 9-61.** (a) $\chi^2_0 = 1.72$, do not reject H_0
(b) $0.5 < P$ -value < 0.9
- 9-63.** (a) $\chi^2_0 = 1.053$, do not reject H_0
(b) $0.1 < P$ -value < 0.5

Section 9-8

- 9-65.** (a) $\chi^2_0 = 11.65$, do not reject H_0
(b) $0.05 < P$ -value < 0.10
- 9-67.** (a) $\chi^2_0 = 25.55$, reject H_0
(b) P -value < 0.005
- 9-69.** (a) $\chi^2_0 = 10.71$, do not reject H_0
(b) $0.05 < P$ -value < 0.10

Supplemental

- 9-71.** (a) $p(1 - p)/50$
(b) $p(1 - p)/80$
(c) $p(1 - p)/100$
- 9-73.** (a) $\beta = 0.564$
(b) $\beta = 0.161$
(c) $\beta = 0.116$
- 9-75.** (a) 0.61026 (b) 0.995
(c) 0.9988
- 9-79.** (a) $\chi^2_0 = 5.546$, reject H_0
(b) $0.01 < P$ -value < 0.025
- 9-81.** (a) $\chi^2_0 = 1.75$, do not reject H_0
- 9-83.** (a) $\chi^2_0 = 17.929$, reject H_0
(b) P -value = 0.0123
- 9-85.** (a) $\chi^2_0 = 63.36$, reject H_0
- 9-87.** (a) $z_0 = -7.32$, reject H_0
(b) P -value $\cong 0$
(c) $\chi^2_0 = 12.0$, reject H_0
- 9-89.** (b) $t_0 = 1.608$, do not reject H_0
(c) $0.1 < P$ -value < 0.2

CHAPTER 10**Section 10-2**

- 10-1.** (a) Yes, cannot reject H_0
(b) P -value = 0.3222
(c) 0.9967
(d) $(-0.0098, 0.00298)$
(e) 9
- 10-3.** 1, Yes
- 10-5.** (a) $(0.0987, 0.2813)$
(b) $(0.0812, 0.299)$
(c) $(-\infty, 0.2813)$
- 10-7.** (a) $(-3.684, -2.116)$
(b) $z_0 = -7.254$ reject H_0
(c) P -value $\cong 0$
- 10-9.** 11
- 10-11.** (a) $(-5.83, -0.57)$ (b) Yes
- 10-13.** $z_0 = -2.385$, reject H_0
- 10-15.** Yes

Section 10-3

- 10-17.** (a) $t_0 = 0.230$, do not reject H_0
(b) P -value > 0.80
(c) $(-0.394, 0.494)$
- 10-19.** (a) $t_0 = -3.11$, reject H_0
(b) $(-5.688, -0.3122)$
- 10-21.** (a) $t_0 = -2.83$, reject H_0
(b) $0.010 < P$ -value < 0.020
(c) $(0.111, 0.749)$
- 10-23.** (17.235, 44.765)
- 10-25.** $t_0 = -5.499$, P -value < 0.0010
- 10-27.** (a) $t_0 = 3.03$, reject H_0
(b) $0.005 < P$ -value < 0.010
(c) $t_0 = 3.03$, reject H_0

10-29. $(-14.34, 21.94)$

- 10-31.** (b) $t_0 = 2.558$, reject H_0
(c) P -value $\cong 0.020$
(d) 0.05 (e) $n = 51$
(f) $(1.86, 18.94)$

Section 10-4

- 10-33.** $(0.1694, 0.3778)$
- 10-35.** $t_0 = 0.357$, cannot reject H_0
- 10-37.** $(-727.46, 2464.21)$
- 10-39.** $t_0 = 5.465$, reject H_0
- 10-41.** $t_0 = 8.387$, reject H_0
- 10-43.** $t_0 = 3.45$, reject H_0

Section 10-5

- 10-45.** (a) 1.59 (b) 2.28 (c) 2.64
(d) 0.529 (e) 0.524
(f) 0.311
- 10-47.** $f_0 = 0.657$, cannot reject H_0
- 10-49.** No
- 10-51.** (a) $(0.08775, 3.594)$
(b) $(0.0585, 5.3)$
(c) $(0.137, \infty)$
- 10-53.** $f_0 = 0.297$, cannot reject H_0
- 10-55.** $f_0 = 0.2575$, cannot reject H_0
- 10-57.** $(0.3369, 2.640)$
- 10-59.** $f_0 = 0.640$, cannot reject H_0

Section 10-6

- 10-61.** $z_0 = 1.49$, cannot reject H_0
- 10-63.** (a) 0.81859 (b) 383
- 10-65.** (a) $z_0 = 3.42$, reject H_0 ,
 P -value = 0.00062
- 10-67.** $(0.0434, 0.1616)$

Supplemental

- 10-69.** $(1.40, 8.36)$
- 10-71.** (a) $t_0 = 2.554$, reject H_0
(b) $t_0 = 2.554$, cannot reject H_0
(c) $t_0 = -1.986$, cannot reject H_0
(d) $t_0 = -1.986$, cannot
reject H_0
- 10-73.** (a) $z_0 = 6.55$, reject H_0
(b) $z_0 = 6.55$, reject H_0
- 10-75.** (a) $(-0.0335, 0.0329)$
(b) $(-0.0282, 0.0276)$
(c) $(-0.0238, 0.0232)$,
 $(-0.0203, 0.0200)$
- 10-79.** 60
- 10-81.** 26
- 10-83.** (a) No (b) Yes
(d) $(18.124, 294.35)$
- 10-85.** (b) $t_0 = -6.06$, reject H_0
- 10-87.** (b) $t_0 = -0.512$, cannot
reject H_0 (c) 16

- 10-89.** (b) $t_0 = -2.74$, reject H_0
 (c) 0.8 (d) 26

CHAPTER 11

Section 11-2

- 11-1.** (a) $\hat{\beta}_0 = 48.013$, $\hat{\beta}_1 = -2.330$
 (b) 37.99 (c) 39.39 (d) 6.71
- 11-3.** (a) $\hat{\beta}_0 = 0.4631476$,
 $\hat{\beta}_1 = 0.0074902$
 (b) $\hat{\beta}_1 = 0.00749$
- 11-5.** (a) $\hat{\beta}_0 = 13.3202$,
 $\hat{\beta}_1 = 3.32437$,
 $\hat{\sigma}^2 = 8.76775$
 (b) 38.253 (c) -2.0273
- 11-7.** (a) $\hat{\beta}_0 = 33.5348$,
 $\hat{\beta}_1 = -0.0353971$,
 $\hat{\sigma}^2 = 13.392$
 (b) 28.226 (c) 1.50048
- 11-9.** (b) $\hat{\beta}_0 = -9.8131$,
 $\hat{\beta}_1 = 0.171484$,
 $\hat{\sigma}^2 = 1.9818$
 (c) 4.76301
- 11-11.** (b) $\hat{\beta}_0 = 0.470467$,
 $\hat{\beta}_1 = 20.5673$,
 $\hat{\sigma}^2 = 13.81$
 (c) 21.038 (d) 1.6629
- 11-17.** $\hat{\beta}_0 = 0$, $\hat{\beta}_1 = 21.031461$

Section 11-5

- 11-19.** (a) $f_0 = 73.95$, $P\text{-value} = 0.000001$, reject H_0
 (b) $se(\hat{\beta}_1) = 0.0004839$,
 $se(\hat{\beta}_0) = 0.04091$
- 11-21.** (a) $t_0 = 8.518$, reject H_0
 (b) $f_0 = 72.5563$, reject H_0
 (c) $se(\hat{\beta}_1) = 0.3902$,
 $se(\hat{\beta}_0) = 2.5717$
 (d) $t_0 = 5.2774$, reject H_0
- 11-23.** (a) $f_0 = 4.53158$, do not reject H_0 , $P\text{-value} = 0.04734$
 (b) $se(\hat{\beta}_1) = 0.0166281$,
 $se(\hat{\beta}_0) = 2.61396$
 (c) $t_0 = 0.87803$, $P\text{-value} = 0.804251$, do not reject H_0
 (d) $t_0 = 12.8291$, $P\text{-value} \cong 0$, reject H_0
- 11-25.** (a) $f_0 = 44.6567$, reject H_0
 $P\text{-value} = 0.000003$
 (b) $se(\hat{\beta}_1) = 0.0256613$,
 $se(\hat{\beta}_0) = 2.13526$
 (c) $t_0 = -4.59573$, reject H_0 ,
 $P\text{-value} = 0.00022$
- 11-27.** (a) $f_0 = 155$, reject H_0
 $P\text{-value} < 0.00001$

- (b) $se(\hat{\beta}_1) = 0.0256613$,
 $se(\hat{\beta}_0) = 2.13526$
 (c) $t_0 = -4.59573$, reject H_0
 $P\text{-value} = 0.00022$
 (d) $t_0 = 57.8957$, reject H_0
 $P\text{-value} < 0.00001$
 (e) $t_0 = 2.7651$, reject H_0
 $P\text{-value} = 0.0064$

Section 11-6 and Section 11-7

- 11-31.** (a) (-2.9175, -1.7421)
 (b) (46.7145, 49.3114)
 (c) (41.3293, 43.0477)
 (d) (38.4289, 46.1281)
- 11-33.** (a) (-0.00961, -0.00444)
 (b) (16.2448, 27.3318)
 (c) (7.91433, 10.37167)
 (d) (4.07214, 14.21386)
- 11-35.** (a) (9.10130, 9.31543)
 (b) (-11.6219, -1.04911)
 (c) (498.72024, 501.52776)
 (d) (495.57344, 504.67456)
- 11-37.** (a) (0.03689, 0.010183)
 (b) (-47.0877, 14.0691)
 (c) (44.0897, 49.1185)
 (d) (37.8298, 55.3784)
- 11-39.** (a) (201.552, 226.590)
 (b) (-4.67015, -2.346960)
 (c) (111.8339, 145.7941)
- 11-41.** (a) (-43.1964, -30.7272)
 (b) (2530.09, 2720.68)
 (c) (1823.7833, 1948.5247)
 (d) (1668.9013, 2103.4067)

Section 11-8

- 11-43.** (d) $R^2 \cong 76.73\%$
- 11-45.** (a) $R^2 = 20.1121\%$
 (c) Yes
- 11-47.** (a) $R^2 = 71.27\%$
- 11-49.** (a) $R^2 = 85.22\%$

Section 11-10

- 11-55.** (a) $\hat{\beta}_0 = -0.0280411$,
 $\hat{\beta}_1 = 0.990987$
 (b) $f_0 = 79.838$, reject H_0
 (c) 0.903 (d) $t_0 = 8.9345$,
 reject H_0
 (e) $z_0 = 3.879$, reject H_0
 (f) (0.7677, 0.9615)
- 11-57.** (a) $r = -0.738027$
 (b) $t_0 = -5.577$, reject H_0 ,
 $P\text{-value} = 0.00000738$
 (c) (-0.871, -0.504)
 (d) $z_0 = -0.394$, do not reject H_0 , $P\text{-value} = 0.6936$

- 11-59.** (a) $t_0 = 5.47$, reject H_0 ,
 $P\text{-value} \cong 0$
 (b) (0.3358, 0.8007) (c) Yes
- 11-61.** (a) $r = 0.933203$
 (b) $t_0 = 10.06$, reject H_0
 (c) $\hat{\beta}_0 = 0.72538$,
 $\hat{\beta}_1 = 0.498081$,
 $f_0 = 101.16$, reject H_0
 (d) $t_0 = 0.468345$, do not reject H_0

Supplemental

- 11-65.** (a) $\hat{\beta}_0 = 93.34$, $\hat{\beta}_1 = 15.64$
 (b) $f_0 = 12.872$, reject H_0
 (c) (7.961, 23.322)
 (d) (74.758, 111.923)
 (e) (126.18, 138.70)
- 11-67.** (b) $\hat{\beta}_0 = -0.8819$,
 $\hat{\beta}_1 = 0.00385$
 (c) $f_0 = 122.03$, reject H_0
 (d) No. (e) $\hat{\beta}_0 = 0.5967$,
 $\hat{\beta}_1 = 0.00097$
- 11-69.** $\hat{y} = 0.7916x$
- 11-71.** (b) $\hat{\beta}_0 = -193$, $\hat{\beta}_1 = 15.296$
 (c) (-4.912, 35.504)
- 11-75.** (b) $\hat{\beta}_0 = 66$, $\hat{\beta}_1 = 0.930$
 (c) $f_0 = 19.79$, reject H_0
 $R^2 = 71.2\%$
 (d) $t_0 = -0.1953$, cannot reject H_0

CHAPTER 12

Section 12-1

- 12-1.** (b) $\hat{\beta} = \begin{bmatrix} 171.054 \\ 3.713 \\ -1.126 \end{bmatrix}$
 (c) 189.481
- 12-3.** (b) 2
- 12-5.** (a) $\hat{y} = 33.4491 - 0.05435x_1 + 1.07822x_2$
 (b) 8.03 (c) 19.30
- 12-7.** (a) $\hat{y} = 383.80 - 3.6381x_1 - 0.1119x_2$
 (b) $\hat{\sigma}^2 = 153.0$, $se(\hat{\beta}_0) = 36.22$,
 $se(\hat{\beta}_1) = 0.5665$,
 $se(\hat{\beta}_2) = 0.04338$
 (c) 180.95
 (d) $\hat{y} = 484.0 - 7.656$
 $x_1 - 0.222$
 $x_2 - 0.0041x_{12}$
 (e) $\hat{\sigma}^2 = 147.0$, $se(\hat{\beta}_0) = 101.3$,
 $se(\hat{\beta}_1) = 3.846$,
 $se(\hat{\beta}_2) = 0.113$,
 $se(\hat{\beta}_{12}) = 0.0039$
 (f) -31.3

- 12-9.** (a) $\hat{y} = 47.174 - 9.7352x_1 + 0.4283x_2 + 18.2375x_3$
(b) 12 (c) $se(\hat{\beta}_0) = 49.5815$, $se(\hat{\beta}_1) = 3.6916$, $se(\hat{\beta}_2) = 0.2239$, $se(\hat{\beta}_3) = 1.312$ (d) 91.43
- 12-11.** $\hat{y} = -8.0119 + 0.494x_1 + 0.0018x_2 + 0.0023x_3 + 0.0383x_4 - 0.2068x_5 - 0.0128x_6 + 0.030x_7 + 0.0407x_8 - 0.2083x_9$
 $\hat{\sigma}^2 = 2.32$, $se(\hat{\beta}_0) = 16.18$, $se(\hat{\beta}_1) = 0.0481$, $se(\hat{\beta}_2) = 0.0064$, $se(\hat{\beta}_3) = 0.0209$, $se(\hat{\beta}_4) = 0.0515$, $se(\hat{\beta}_5) = 0.2611$, $se(\hat{\beta}_6) = 0.0266$, $se(\hat{\beta}_7) = 0.038$, $se(\hat{\beta}_8) = 0.1483$, $se(\hat{\beta}_9) = 0.1110$

Section 12-2

- 12-13.** (a) 260.09, reject H_0
(b) reject H_0 both significant
- 12-15.** (a) $f_0 = 25.7465$, reject H_0
P-value < 0.000001
(b) Reject H_0 , all coefficients are significant
- 12-17.** (a) $f_0 = 53.3162$, reject H_0
(b) Only β_1 is significant
- 12-19.** (a) $f_0 = 10.08$, P-value = 0.005
(b) Only β_1 is significant
- 12-21.** (a) $f_0 = 67.92$, reject H_0
(b) $f_0 = 1.07$, do not reject H_0
(c) 147.0
- 12-23.** (a) $f_0 = 850.55$, reject H_0
(b) Regression coefficients for x_1 and x_3 are significant
- 12-25.** (a) $f_0 = 101.79$, reject H_0
(b) Only regression coefficient for "PTS" is significant
(c) $\hat{y} = -5.531 + 0.497x_{PTS} - 0.004x_{PPG}$, $f_0 = 510.12$
reject H_0 only regressor "PTS" is significant

Section 12-3 and Section 12-4

- 12-27.** (a) $(-0.00657, -0.00122)$
(b) 0.497648 (c) $(7.16, 9.22)$
- 12-29.** (a) $0.0972 \leq \beta_1 \leq 1.4174$, $-1.9646 \leq \beta_2 \leq 17.0026$, $-1.7953 \leq \beta_3 \leq 6.7613$, $-1.7941 \leq \beta_4 \leq 0.8319$

- 12-31.** (a) $-0.595 \leq \beta_2 \leq 0.535$, $0.229 \leq \beta_3 \leq 0.812$, $-0.216 \leq \beta_4 \leq 0.013$, $-7.298 \leq \beta_5 \leq 2.977$
(b) $(7.982, 10.009)$
(c) $(6.8481, 11.143)$
- 12-33.** (a) $-0.00003 \leq \beta_{Temp} \leq 0.00012$, $0.000203 \leq \beta_{Soaktime} \leq 0.00288$, $-0.02306 \leq \beta_{Soakpt} \leq 0.05976$, $0.00501 \leq \beta_{DFtime} \leq 0.01056$, $-0.01969 \leq \beta_{Diffpt} \leq 0.01342$
(b) $(0.0206, 0.0234)$
- 12-35.** (a) $(0.3882, 0.5998)$
(b) $y = -5.767703 + 0.496501x_{pts}$
(c) $(0.4648, 0.5282)$

Section 12-5

- 12-37.** (a) 0.82897 (d) No
- 12-39.** (a) 0.985 (b) 0.99
- 12-41.** (b) 0.9937
- 12-43.** (a) 0.9582 (c) 32
- 12-45.** (a) 0.12
(b) 17 and 18

Section 12-6

- 12-47.** (a) $\hat{y} = -1.633 + 1.232x - 1.495x^2$
(b) $f_0 = 1858613$, reject H_0
(c) $t_0 = -601.64$, reject H_0
- 12-49.** (a) 802.943
(b) $\hat{y} = -26204.14 + 189.09x - 0.331x^2$
- 12-51.** (a) $\hat{y} = -1.769 + 0.421x_1 + 0.222x_2 - 0.128x_3 - 0.02x_1x_2 + 0.009x_1x_3 + 0.003x_2x_3 - 0.019x_1^2 - 0.007x_2^2 + 0.001x_3^2$
(b) $f_0 = 19.628$, reject H_0
(d) $f_0 = 1.612$, do not reject H_0

- 12-55.** (a) Min. MS_E : $x_1, x_3, x_4, x_5, x_7, x_8, x_{10}$, $MS_E = 6.58$, $C_p = 5.8$, Min. C_p : x_5, x_8, x_{10} , $C_p = 5.02$, $MS_E = 7.97$
(b) $\hat{y} = 34.434 - 0.048x_1$, $MS_E = 8.81$, $C_p = 5.55$
(c) Same as part (b)
(d) $\hat{y} = 0.341 + 2.862x_5 + 0.246x_8 - 0.010x_{10}$, $MS_E = 7.97$, $C_p = 5.02$

- 12-57.** (a) $y = 4.656 + 0.511x_3 - 0.124x_4$

- (b) Same as part (a)
(c) Same as part (a)
(d) All models are the same

- 12-59.** (a) $\hat{y} = -0.304 + 0.083x_1 - 0.031x_3 + 0.004x_2^2$, $C_p = 4.04$, $MS_E = 0.004$

- (b) $\hat{y} = -0.256 + 0.078x_1 + 0.022x_2 - 0.042x_3 + 0.0008x_3^2$, $C_p = 4.66$, $MS_E = 0.004$

- 12-61.** (a) Min. C_p : x_1, x_9 , $C_p = -1.67$
(b) Min. MS_E : x_1, x_7, x_9 , $MS_E = 1.67$, $C_p = -0.77$
(c) Max. adjusted R^2 : x_1, x_7, x_9 , Adj. $R^2 = 0.98448$

Supplemental

- 12-65.** (a) $f_0 = 1323.62$, reject H_0
P-value < 0.00001

- (b) Only regressor x_4 is significant H_0

- 12-67.** (a) $\hat{y} = -0.908 + 5.482x_1^* + 1.126x_2^* - 3.920x_3^* - 1.143x_4^*$

- (b) $f_0 = 109.02$, reject H_0 , all regressors are significant

- 12-69.** (a) $\hat{y} = -3982.1 + 1.0964x_1 + 0.1843x_3 + 3.7456x_4 + 0.8343x_5 - 16.2781x_6$, $MS_E(p) = 694.93$, $C_p = 5.62$

- (b) $\hat{y} = -4280.2 + 1.442x_1 + 0.209x_3 + 0.6467x_5 - 17.5103x_6$, $MS_E(p) = 714.20$, $C_p = 5.57$
(c) Same as model b

- 12-71.** $VIF(\hat{\beta}_3^*) = 51.86$, $VIF(\hat{\beta}_4^*) = 9.11$, $VIF(\hat{\beta}_5^*) = 28.99$

- 12-73.** (a) $f_0 = 18.28$, reject H_0
(b) $f_0 = 2$, do not reject H_0

CHAPTER 13**Section 13-2**

- 13-1.** (a) Reject H_0
(b) Model is satisfactory

- 13-3.** (a) Reject H_0 (b) P-value $\equiv 0$

- 13-5.** (a) Reject H_0 (c) $(140.71, 149.29)$, $(7.36, 24.14)$

- 13-7.** (a) Do not reject H_0
(b) P-value = 0.214

- 13-9.** (a) Reject H_0
(b) P-value = 0.002

- (d) (69.17, 81.81)
 (e) (8.42, 26.33)
- 13-19.** 5

Section 13-3

- 13-21.** (a) Reject H_0 (b) 0.01412
 (c) 0.0148
- 13-23.** (a) Do not reject H_0 (b) 0
 (c) 24

Section 13-4

- 13-25.** (a) Reject H_0
13-27. (a) Do not reject H_0
13-29. (a) Do not reject H_0

Supplemental

- 13-31.** (a) Reject H_0
 (c) (132.97, 147.83)
- 13-35.** (a) Reject H_0
 (b) P -value = 0.007
- 13-37.** (a) Reject H_0
- 13-39.** (a) 0.85 (b) 5

CHAPTER 14

Section 14-4

- 14-1.** (a) Reject H_0 for both main effects and the interaction
- 14-3.** (a) Reject H_0 for main effects
- 14-7.** (-3.40, 7.64)
- 14-9.** (a) Reject H_0 for both main effects and the interaction

Section 14-5

- 14-11.** (a) All these main effects are significant and the hardwood concentration-freeness interaction is significant at $\alpha = 0.05$. The P -value for the hardwood-cooking time interaction is 0.075, it is possibly an important effect as well.

Section 14-7

- 14-13.** (a) Reject H_0 for factors B , C , and AC
 (b) $\hat{y} = 413.125 + 9.125x_1 + 45.12x_2 + 35.87x_3 - 59.62x_1x_3$
- 14-15.** $\hat{y} = 175.25 - 4.12x_1 + 5.19x_2 + 0.19x_4 + 4.62x_1x_4$
- 14-17.** (b) Reject H_0 for factor B
- 14-19.** (a) Factors A , B , C , and AB

- 14-21.** (b) Factors A , B , and AB
 (c) $\hat{y} = 400 + 40.124x_1 - 32.75x_2 + 26.625x_1x_2$

Section 14-8

- 14-23.** Block 1: (1) $ab ac bc$
 Block 2: $a b c abc$
 There are no significant factors
- 14-25.** Block 1: (1) $ac bd abcd$
 Block 2: $a c abd bcd$
 Block 3: $b abc d acd$
 Block 4: $ab bc ad cd$
 Factor A is significant

- 14-27.** Block 1: (1) $ab de acd bcd ace bce abde$
 Block 2: $a b cd ce ade bde abce abcd$
 Block 3: $d e bc bd abd abe acde bcde$
 Block 4: $c ad ae bd be abc cde abcde$

- 14-29.** (a) Factors A , C , AB , and AC are significant

Section 14-9

- 14-31.** (a) Factors A , B , and D are significant
 (c) Factors A , B , D , AB , and AD are significant
- 14-33.** (b) Design Generators: $D = AB$, $E = AC$; Defining Relation: $I = ABD = ACE = BCDE$; Aliases: $A = BD = CD = ABCDE$, $B = AD = CDE = ABCE$, $C = AE = BDE$, $D = AB = BCE$, $E = AC = BCD$, $BC = DE$, $BE = CD$
- 14-35.** 2^{4-1} replicated twice
- 14-37.** Factors A , B , and D are significant
- 14-39.** Design Generators: $D = AB$, $E = AC$, $F = BC$; Defining Relations: $I = ABD = ACE = BCF = BCDE = ACDF = ABEF = DEF$; Aliases: $A = BD = CE$, $B = AD = CF$, $C = AE = BF$, $D = AB = EF$, $E = AC = DF$, $F = BC = DE$, $AB = EF$, $AF = BE = CD$

Supplemental

- 14-41.** The main effect of pH and the interaction of pH and

Catalyst Concentration are significant

- 14-43.** The salts, application levels, and the interaction between salts and application levels are significant
- 14-45.** There are no significant factors
- 14-47.** (a) The factors V , P , G , and PG are significant. Effects $P = -10.75$, $V = 15.75$, $G = -25.00$, $PG = 19.25$
 (b) $\hat{y} = 102.75 + 7.88x_1 - 5.37x_2 - 12.50x_4 + 9.62x_2x_4$

- 14-49.** The factors V and G are significant at $\alpha = 0.10$. $\hat{y} = 100.63 - 14.12x_1 - 13.13x_4$

- 14-51.** Design Generators: $D = \pm AB$, $E = \pm AC$; Defining Relations: $I = ABD = ACE = BCDE$; Aliases: $A = BD = CE$, $B = AD = CDE$, $C = AE = BDE$, $D = AB = BCE$, $E = AC = BCD$, $BC = DE$, $BE = CD$

- 14-53.** (a) $E = ABCD$ (b) Factors A , B , C , E , and interaction BE are significant (c) Factor A is significant in affecting variability

CHAPTER 15

Section 15-2

- 15-1.** Do not reject H_0 , P -value = 0.109
- 15-3.** Reject H_0 , P -value = 0.0002
- 15-5.** (a) Do not reject H_0
 (b) $z_0 = 0.577$, P -value = 0.281
- 15-7.** $z_0 = -1.34$, do not reject H_0 , P -value = 0.1802
- 15-9.** Do not reject H_0
- 15-11.** $z_0 = 2.24$, reject H_0
- 15-13.** Reject H_0
- 15-15.** $z_0 = 2.84$, reject H_0
- 15-17.** (a) 0.025 (b) 0.115
 (c) 0.011 (d) 0.1587
- 15-19.** P -value = 0.04

Section 15-3

- 15-21.** $w = 71 > 52$, do not reject H_0
- 15-23.** $w = 8 < 65$, reject H_0
- 15-25.** $w = 25 < 52$, reject H_0
- 15-27.** $w = 1 < 25$, reject H_0

Section 15-4

- 15-29.** $w = 38 > 23$, do not reject H_0

15-31. $z_0 = -2.78$, do not reject H_0 ,
 $P\text{-value} = 0.9973$

15-33. $w = 55 < 78$, reject H_0

15-35. $z_0 = -3.77$, reject H_0 ,
 $P\text{-value} = 0.0001$

Section 15-5

15-37. Reject H_0

15-39. Do not reject H_0

15-41. $P\text{-value} = 0.018$

Supplemental

15-43. Do not reject H_0 , $P\text{-value} \approx 1$

15-45. Do not reject H_0

15-47. Do not reject H_0

15-49. Reject H_0

15-51. Reject H_0

15-53. Reject H_0

15-55. Reject H_0 , $P\text{-value} \approx 0$

15-57. Reject H_0 , $P\text{-value} = 0.009$

CHAPTER 16

Section 16-5

16-1. (a) \bar{x} chart: $UCL = 37.5789$,
 $CL = 34.32$, $LCL = 31.0611$
 R chart: $UCL = 11.9461$,
 $CL = 5.65$, $LCL = 0$

(b) 1 point outside limits on
 \bar{x} chart. Revised limits:
 \bar{x} chart: $UCL = 37.4038$, $CL = 34.0947$, $LCL = 30.7857$,
 R chart: $UCL = 12.1297$,
 $CL = 5.7368$, $LCL = 0$

16-3. (a) \bar{x} chart: $UCL = 17.40$,
 $CL = 15.09$, $LCL = 12.79$
 R chart: $UCL = 5.792$,
 $CL = 2.25$, $LCL = 0$

(b) \bar{x} chart: $UCL = 17.96$,
 $CL = 15.78$, $LCL = 16.62$
 R chart: $UCL = 5.453$,
 $CL = 2.118$, $LCL = 0$

(c) \bar{x} chart: $UCL = 17.42$,
 $CL = 15.09$, $LCL = 12.77$
 s chart: $UCL = 3.051$,
 $CL = 1.1188$, $LCL = 0$
revised limits: \bar{x} chart:
 $UCL = 17.95$, $CL = 15.78$,
 $LCL = 13.62$, s chart:
 $UCL = 2.848$, $CL = 1.109$,
 $LCL = 0$

16-5. (a) \bar{x} chart: $UCL = 242.78$,
 $CL = 223$, $LCL = 203.22$
 R chart: $UCL = 72.51$,
 $CL = 34.286$, $LCL = 0$

(b) $\hat{\mu} = 223$, $\hat{\sigma} = 14.74$
(a) \bar{x} chart: $UCL = 0.06347$,

$CL = 0.06294$,

$LCL = 0.0624$ R chart:

$UCL = 0.001954$,

$CL = 0.000924$, $LCL = 0$

(b) \bar{x} chart: $UCL = 0.06346$,
 $CL = 0.06295$,

$LCL = 0.06241$ s chart:

$UCL = 0.000766$,

$CL = 0.000367$, $LCL = 0$

(c) The points are 1, 5, 14, 17,
20, 21, and 22; or outside
the control limits of the
 R chart: 6 and 15

Section 16-6

16-9. (a) I chart: $UCL = 60.8887$,
 $CL = 53.05$, $LCL = 45.2113$
 MR chart: $UCL = 9.63382$,
 $CL = 2.94737$, $LCL = 0$

(b) $\hat{\mu} = 53.05$, $\hat{\sigma} = 2.613$

16-11. (a) I chart: $UCL = 10.5358$,
 $CL = 10.0272$,
 $LCL = 9.51856$ MR chart:
 $UCL = 0.625123$,

$CL = 0.19125$, $LCL = 0$

(b) $\hat{\mu} = 10.027$, $\hat{\sigma} = 0.1696$

Section 16-7

16-13. (a) $PCR = PCR_k = 1.5$

(b) 0

16-15. (a) 0.00075 (b) $PCR = 1.13$,
 $PCR_k = 1.104$

16-17. (a) $PCR = PCR_k = 1.18$

(b) 0.00046

16-19. (a) 0.0009 (b) $PCR = 1.13$,
 $PCR_k = 1.06$

16-21. $PCR = 0.50$, $PCR_k = 0.357$

16-23. $PCR = 0.49$, $PCR_k = 0.474$

Section 16-8

16-25. (a) U chart: $UCL = 3.811$,
 $CL = 1.942$, $LCL = 0.0722$

(b) Revised limits: U chart:

$UCL = 3.463$,

$CL = 1.709$, $LCL = 0$

16-27. (c) chart: $UCL = 19.06$,
 $CL = 9.708$, $LCL = 0.3609$

Section 16-9

16-29. (a) 0.2177 (b) 4.6

16-31. (a) 0.1020 (b) 9.8

16-33. (a) 0.0548 (b) 18.25

16-35. (a) 0.1515 (b) 6.6

16-37. (a) 0.16603 (b) 6.02

Section 16-10

16-39. (a) $\hat{\sigma} = 0.1695$

16-41. (a) ARL = 38.0

(b) ARL = 10.4

Supplemental

16-43. (a) \bar{x} chart: $UCL = 64.0181$,
 $CL = 64.0$, $LCL = 63.982$
 R chart: $UCL = 0.0453972$,
 $CL = 0.01764$, $LCL = 0$

(b) $\hat{\mu} = 64$, $\hat{\sigma} = 0.0104$

(c) $PCR = 0.641$,

(d) $PCR_k = 0.641$

(e) $\sigma^2 = 0.025$,

(f) 0.1705, ARL = 5.87

16-45. (a) p chart: $UCL = 0.20387$,
 $CL = 0.11$, $LCL = 0.01613$

(b) p chart: $UCL = 0.1717$,
 $CL = 0.106$,

$LCL = 0.04092$

16-47. (a) c chart: $UCL = 7.51442$,
 $CL = 2.64$, $LCL = 0$

(b) c chart: $UCL = 6.50924$,
 $CL = 2.1304$, $LCL = 0$

16-49. (b) 6.30 (c) 2

16-51. (a) \bar{x} chart: $UCL = 140.168$,
 $CL = 139.49$,

$LCL = 138.812$ R chart:

$UCL = 2.48437$,

$CL = 1.175$, $LCL = 0$

(b) Revised control limits: \bar{x} chart:
 $UCL = 140.518$,
 $CL = 139.808$,

$LCL = 139.098$ R chart:
 $UCL = 2.6023$,

$CL = 1.231$, $LCL = 0$

(c) $PCR = 1.26$, $PCR_k = 1.14$

(d) $\sigma^2 = 0.091$

(e) 0.1877, ARL = 5.33

16-53. (a) 0.96995 (b) 1

16-57. 0.000135